Global Crack Detection using Bispectral Analysis

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A global non-destructive testing technique for detecting cracks in engineering parts has been developed. The technique uses the bispectrum to analyse the mixing of two ultrasonic sinusoidal waves in a sample. The bispectrum's insensitivity to noise allows more sensitive detection of mixing signals than the power spectrum. Two sinusoidal signals are generated by signal generators, amplified and applied to a piezo-ceramic disk bonded to a sample. The sample is excited at very-high-order modes of vibration. The response of the sample is measured by a second piezo-ceramic disk and the received signal analysed using the bispectrum signal-processing technique. Frequency mixing occurs as a result of the non-linear behaviour of cracks in the structure. Experiments with fatigue-cracked steel beams demonstrate that fatigue cracks produce a strong mixing effect and that the bispectrum signal relating to the frequency mixing is sensitive to the length of the crack; allowing the quantification of the crack length. Progress is being made in applying the technique to more practical situations: the sensitivity of the technique to transducer position and the input signal parameters (frequency and amplitude) is quantified experimentally.

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1. Introduction

This paper describes the use of ultrasonic acoustic modulation as a method of detecting cracks in metal parts. The current work looks to extend our knowledge of the parameters affecting the technique first described by Hillis et al.[1]. The technique uses bispectral analysis to measure the mixing signal caused by the nonlinear behaviour of a sample excited with two continuous ultrasonic signals.

The nonlinear nature of crack-face contact behaviour can lead to the production of harmonics [2] and, where two frequencies are present, signals at the sum and difference frequencies [3, 4]. Attempts to use these effects to detect cracks have typically concentrated on using the power spectrum to quantify the signals produced by the nonlinear behaviour, although the advantages of the bispectrum in detecting quadratically-phase-coupled signals [5-9] has lead to some interest in using the bispectrum in crack detection [10-14]. As the increase in crack length results in an increase in the bispectrum value corresponding to the mixing frequency [1] that bispectrum value is useful as a measure of the damage.

1.1 Experimental Setup

A 400 mm × 60 mm × 60 mm mild steel beam is excited using a piezo-ceramic disk (diameter 15mm, thickness 2mm) bonded with cyanoacrylate to the sample and driven by a power amplifier connected to two function generators; each supplying a sinusoidal input so that the signal is the superposition of two sine waves. The signal is detected by a second piezo-ceramic disk (diameter 5mm, thickness 2mm) and recorded using a digital oscilloscope. Figure 1 shows the experimental setup.

The samples were suspended using looped wires running under the samples approximately 5cm from either end. Four samples were used: one undamaged and three with fatigue cracks of 5mm, 15mm and 25mm respectively.

Frequencies in the range 100–500 kHz were used, with the conditions that the higher frequency (F_2) was not an integer multiple of the lower (F_1) and the difference between the frequencies was greater than 100 kHz. In order to achieve sufficient signal strength each frequency was tuned to find local maxima in the output amplitude, corresponding to a stationary state of the system. The amplitude of each input signal was then adjusted to give equal output voltages at each driving frequency.

Figure 1: Experimental set-up.

1.2 The Bispectrum

Consider a time-domain signal, $S(t)$, with the Fourier transform $A(f)$. The power spectrum is

$$P(f) = E[A(f)A^*(f)] \quad (1)$$

and the bispectrum is

$$B(f_1, f_2) = E[A(f_1)A(f_2)A^*(f_1+f_2)] \quad (2)$$

where $E[\cdot]$ is the expectation value operator and $A^*(f)$ denotes the complex conjugate of the Fourier transform. In the current work the bispectrum is estimated directly by recording a long signal that is divided into N shorter records labelled n ($= 1, 2, \dots, N$). The Fourier transform, $A_n(f)$, of each record is then calculated and the bispectrum is estimated as $A_n(f_1)A_n(f_2)A_n^*(f_1+f_2)$ averaged over the N records [12, 13].

For a given pair of frequencies f_1 and f_2 there are four conditions for a non-zero bispectrum:

$$\begin{aligned} A(f_1) &\neq 0 \\ A(f_2) &\neq 0 \\ A(f_1 + f_2) &\neq 0 \\ \phi_3 &= \phi_1 + \phi_2 \end{aligned} \quad (3)$$

where ϕ_1 and ϕ_2 are the phases of the signals at f_1 and f_2 respectively and ϕ_3 is the phase of the signal at $f_1 + f_2$.

Figure 2: Bispectrum resulting from exciting 60 mm $\times$ 60 mm $\times$ 400 mm steel sample at 269kHz and 473kHz. A nonzero signal in the bispectrum (white indicates zero bispectrum in the plot) occurs where there is signal at three frequencies, f_1, f_2 and $f_1 + f_2$. The peaks on the $f_1 = f_2$ line result from second harmonic generation. The peaks at 269 kHz, 204 kHz and 473 kHz, 269 kHz result from signals at the sum and difference frequencies respectively.

2. Experimental Results

Figure 3: Bispectrum peak at $F_1, F_2 - F_1$ from signal detected in steel beams with fatigue cracks of different lengths.

Samples were excited at 270 kHz and 473 kHz such that the output signal at each driving frequency is 1V (solid line), 2V (---), 3V (- -) and 4V (- - -).

The samples were excited as described in section 1.1. The resulting bispectra took the form shown in figure 2 (note that some frequency smoothing has been performed for the sake of clarity), which shows the results for the 5mm-cracked sample excited at 269kHz and 473kHz with outputs at those frequencies of 1V peak-to-peak. As the two frequencies are interchangeable the plot has reflection symmetry along $f_1 = f_2$. The peaks on that line correspond to harmonic frequencies of the inputs combining with the input signals to conform with eqn. 3. The off axis peaks correspond to the sum and difference frequencies. At no other point are the conditions of eqn. 3 met and so the bispectrum is zero at all other points. Hillis et al. [1] demonstrated that for a given set of parameters the value at $F_1, F_2 - F_1$ is a useful measure of the sample damage: figure 3 shows that this is true across a range of vibration amplitudes (as measured by the voltage produced in the piezo-ceramic disk). The increase in the size of the peaks with increasing applied vibration amplitude closely follows the relationship $B(F_1, F_2 - F_1) \propto V^3(F_1)$, where $V(F_1) = V(F_2)$ is the voltage to which the output signal amplitudes at F_1 and F_2 are set.

A number of factors affect the choice of applied frequencies. Experimental factors limit the range over which the current equipment allows generation and detection, without introducing significant nonlinearity, to 100kHz to 500kHz. The frequencies at which it is possible to obtain a sufficient response are limited by the input and output transducer impulse response function and the modal behaviour of the sample itself. In order to test the validity of the technique at different frequencies a frequency region obeying all those conditions was required over which the frequency could be varied. With the lower

frequency, F_1 , held constant at 200kHz, and adjusting the applied voltage such that the detected signal at F_1 and F_2 was 1V peak-to-peak, the upper frequency, F_2 , was increased from 290kHz to 370kHz in 10kHz increments. This process was repeated for the undamaged and least damaged (5mm fatigue cracked) samples and the resulting bispectrum amplitude at F_1, F_2-F_1 is shown in figure 4. The damaged sample consistently produced a larger signal than the undamaged, indicating that the technique is applicable over a range of frequencies. There is a variation in the degree of increase caused by the crack depending on the frequency, indicating that some frequency pairs will be more effective than others; however the increase at higher frequencies is due to approach of the mixing frequency (F_2-F_1) to 200kHz (the lower driving frequency) rather than an increase in the amount of mixing.

Figure 4: Variation of Bispectrum at F_1, F_2-F_1 with F_2 varied. $F_1 = 200\text{kHz}$ and the output voltage at each driving frequency was set to 1V peak to peak.

The transducer positions shown in figure 1 were chosen on the assumption that they would excite and detect modes with strains perpendicular to the crack surfaces. This would be expected to produce a strong clapping non-linear behaviour. This hypothesis was tested by using transducers at two other positions, shown schematically in figure 5 alongside the resulting bispectrum peak values at F_1, F_2-F_1 . Configuration A places both transducers on one side of the sample (we denote the smaller $60\text{mm} \times 60\text{mm}$ surfaces ‘ends’ and the $60\text{mm} \times 400\text{mm}$ surfaces ‘sides’) with the input transducer 40mm from the end and the receiving transducer 50mm from the input (90mm from the end). Configuration B places both transducers on one side of the sample with the input transducer 40mm from the end and the receiving transducer 320mm from the input. For comparison the results using the previous set-up are also shown, and the original, end-to-end configuration labelled configuration C. Each configuration was tested on all four samples with the peak-to-peak output amplitudes set to 1V. Configurations B and C were driven at 269kHz and 473kHz,

but for configuration A it was found that the response of the system was too small at 473kHz to produce viable results and so 269kHz and 440kHz were used.

Configuration A showed similar results to configuration C for the undamaged sample and the sample with the smallest crack, but higher values for both longer cracks. Configuration B behaved similarly to the original set-up (configuration C) at all crack lengths, but with larger bispectrum values and better contrast between crack lengths. For all three configurations there is a measurable increase in the peak as the crack length is increased.

Figure 5: Variation of Bispectrum at $F_1, F_2 - F_1$ with Increasing Crack Length for Three Different Transducer Set Ups. The three set ups were: Transducers positioned on ends of sample (—), transducers 32cm apart on the side of the sample (---), both using $F_1 = 270\text{kHz}$ and $F_2 = 474\text{kHz}$, and transducers placed on the side, separated by 4cm and excited using $F_1 = 270\text{kHz}$ and $F_2 = 440\text{ kHz}$ (---).

The mixing signals are similar, or higher, for configurations A and B, where the input transducer primarily oscillates parallel to the crack, than the original configuration, where the transducer operates perpendicular to the crack. This indicates that either the position of the transducer does not allow for straightforward selection of modes active in one direction, or the direction in which the stress acts does not affect the nonlinearity of the crack in the expected manner. Work is ongoing to measure the strain at the crack in order to determine the relationship between the strain at the crack and nonlinearity.

3. Conclusions

The bispectrum provides a useful tool to measure the mixing signal produced by nonlinearity in an ultrasonic experiment. The technique, exciting the sample with two ultrasonic frequencies and measuring the difference signal, proves consistent over a range of applied frequencies and vibrational amplitudes and works for a number of different excitation and detection positions. The different responses resulting from different transducer positions raises questions about how the vibrations interact with the crack, which will be addressed in our ongoing work to characterise better the behaviour, near the crack, of the vibrational modes excited, using modelling and strain measurements.

4. References

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