

Defects Evaluation in Lamb Wave Testing of Thin Plates

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Abstract

In the present study, dispersion and displacement curves of ultrasonic lamb wave, propagated in Aluminum thin plates, were drawn. Two ultrasonic lamb wave techniques, pulse-echo (a₁ mode as emitter) and emission (s₁ mode as emitter), were used for interpretation of notch defects with depths of 10%, 30% and 60% of plate thickness. Thickness of plate was 2 mm and the nominal centre frequency of transducers was 2 MHz. It was observed that these techniques are sensitive to evaluate defects, especially in short probe to defect distances. Also, it was found that amplitude analysis can give some qualitative and quantitative information about defects depth. But evaluation results were not sometime repeatable. The basic of evaluation was using a special DAC curve which was easy for applying by operators. In this respect, pulse echo method resulted in better sensitivity of amplitude to defects depth and distance variations as compared to emission method.

Key words: Lamb Wave; Thin plates; Defect Evaluation; DAC curves

Introduction

Ultrasonic lamb wave testing are being used for interpretation of plates [1], multilayer structures [2], pipes[3], rails [4], elbows [5], honeycomb structures [6], composite plates [2], and so on; also for materials characterization (mainly elastic modules and stiffness constants) [7]. It can be used successfully for insulated [8] and coated pipes [9] as well as for inspection of objects under the water [10]. Lamb wave is a special kind of guided wave which can be travel over a long distance. The sensitivity of lamb wave to defects is greater than common ultrasonic method [11]. Lamb wave inspection is fast and its cost is so lower than common ultrasonic techniques or other inspection methods [3, 10, 11]. Angle probes, electromagnetic acoustic transducers [11], comb probe [12], immersion method [13] and laser ultrasonic technique [14] may be used for ultrasonic lamb wave testing. The most difficulty of lamb wave inspection is the dispersive nature of lamb wave and its multimode propagation and so need to signal processing as well as experienced operators [11, 15]. Time-frequency analysis using Wavelet transform [15], Fast Fourier transform and Short Time Fourier transform [16] may be used for signal processing when different lamb modes were overlapped.

The aim of present study is to evaluate defects in thin Aluminum plates. For this aim, two techniques of lamb wave testing (pulse-echo and emission), with different lamb modes as transmitter and receiver, have been used and the sensitivity of these methods to defects depth variations has been compared with each other.

Theory

The ultrasonic waves propagate in two main kinds in materials:

- 1- Longitudinal ultrasonic wave (L): displacement of particles is parallel with the energy transport direction
- 2- Shear ultrasonic wave (S): displacement occurs in the direction perpendicular to energy transport

Shear wave, as shown in Figure 1, can propagate in two main modes:

- a- Shear horizontal wave (SH): displacement describes in the direction parallel to plate surface
- b- Shear vertical wave (SV): displacement occurs in the direction perpendicular to the plate surface

In a free solid elastic thin plate (up to a few wavelengths of bulk ultrasonic wave thick), longitudinal wave are polarized in the direction perpendicular to the surface and SV wave formed and combined with L wave. These combined SV+L is known as lamb wave [17]. In an isotropic plate, lamb waves are either symmetric (s_i) or antisymmetric (a_i). The symmetric modes associate with a compressional rarefaction expansion of the plate and antisymmetric modes associated with a flexural propagation [11, 17]. Lamb wave has a dispersive nature and its phase and group velocities not only depend on the material characterization but also depend on the thickness, frequency and lamb wave mode.

When normal and shear stresses in the surface of plate reach to zero, then lamb wave can propagate [11, 17]. The potential method is the most common approach for solving the lamb wave problems [18, 19]. The effect of thickness, frequency and different modes of lamb wave on the phase and group velocity is defined in dispersion curves. For a single layer plate, the dispersion curves can be plotted by assessment the general dispersion equation, in a manner as defined in Appendix 1. The dispersion curves for an Aluminum plate are shown in Figures 2a and 2b. It can be seen that at least two modes of lamb wave can propagate in a plate. Also lamb modes, except to a_0 and s_0 , have a cut-off frequency. So, for producing a special lamb mode the frequency should be higher than its cut-off frequency and via versa.

For a successful lamb wave testing, it is necessary to draw the dispersion curves. Any point on dispersion curves can be used for ultrasonic testing, but any mode of lamb wave is more sensitive to a special defect type [11]. Some modes are sensitive to coating or surface defects and some modes are sensitive to internal defects, and so on. Displacement curves can explain the sensitivity of lamb modes to defect types [9]. Incident angle and frequency are two parameters which can be varied for excitation a desired lamb wave testing. In the most researches, the frequency has been set for excitation two or three modes, which causing lower dispersion and easier inspection. Snell's law can be used for calculating the incident angle of the media between the transducer and plate for producing a special lamb mode with a defined phase velocity as is followed:

$$\frac{C_{Lm}}{C_p} = \sin \theta_m \quad (1)$$

where C_{Lm} is the velocity of longitudinal ultrasonic wave in the separating media, C_p is the phase velocity of lamb wave mode and θ_m is the incident angle in the separating media. The incident angle in water for immersion testing and in Perspex for variable angle probe has been shown in Figures 3a and 3b.

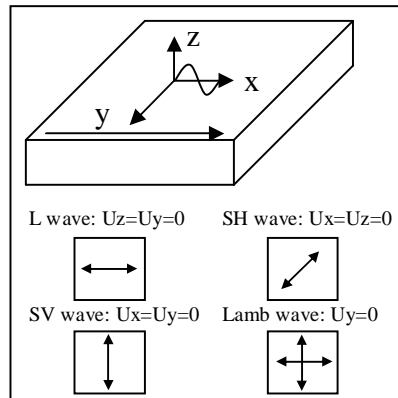


Figure 1: Schematic illustration of ultrasonic wave modes

In multilayer materials as compared with a single layer material, further modes propagate and these modes are neither symmetric nor antisymmetric [18, 19]. Plotting the dispersion and displacement curves is also necessary for employing a successful lamb wave testing in multilayer plates. The transfer matrix methods may be applied for drawing the displacement profile of particles in plate when lamb wave propagate [20]. The dispersion curves in this method can be calculated in the manner as defined by Pan [9, 21]. The displacement curves which are obtained by

this method have been shown in Figures 4a and 4b. The mode of Figure 4a is interested for interpretation of internal defects of plate and the mode of Figure 4b is desired for evaluation of discontinuities and delaminating in the interface of two layers.

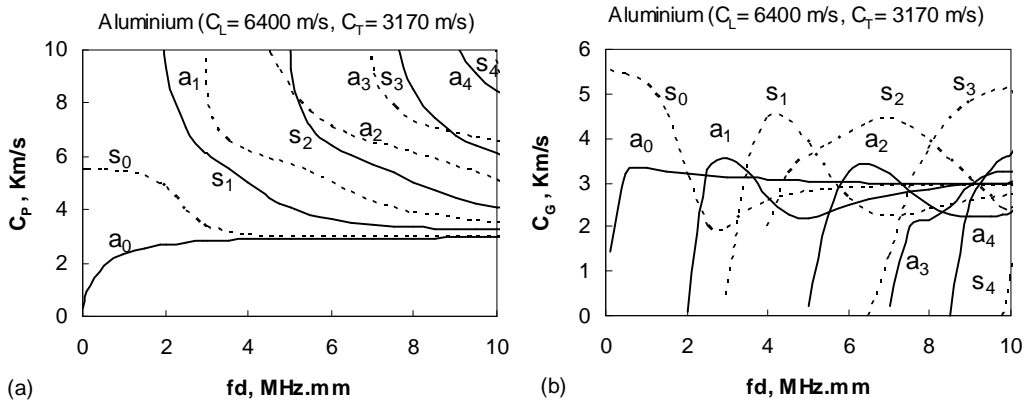


Figure 2: Lamb wave a) phase and b) group velocity dispersion curves, propagated in Aluminum plates

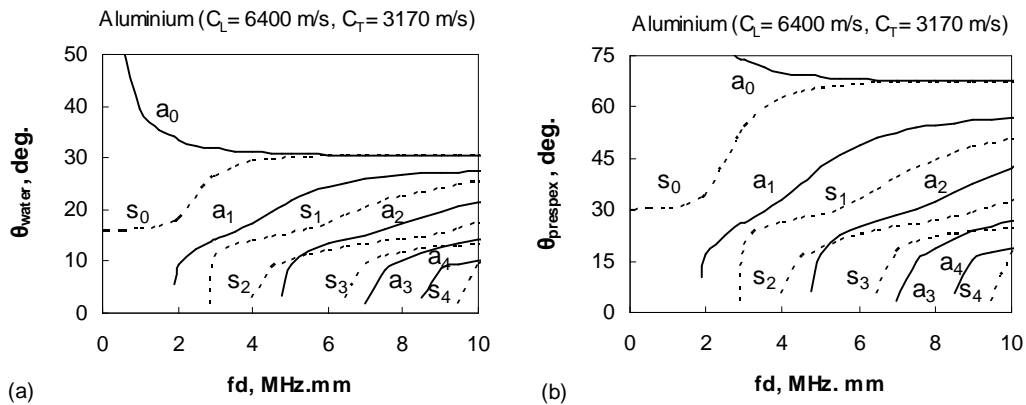


Figure 3: The variations of incident angle in a) Water and b) Perspex for producing different lamb wave modes in Aluminum plates

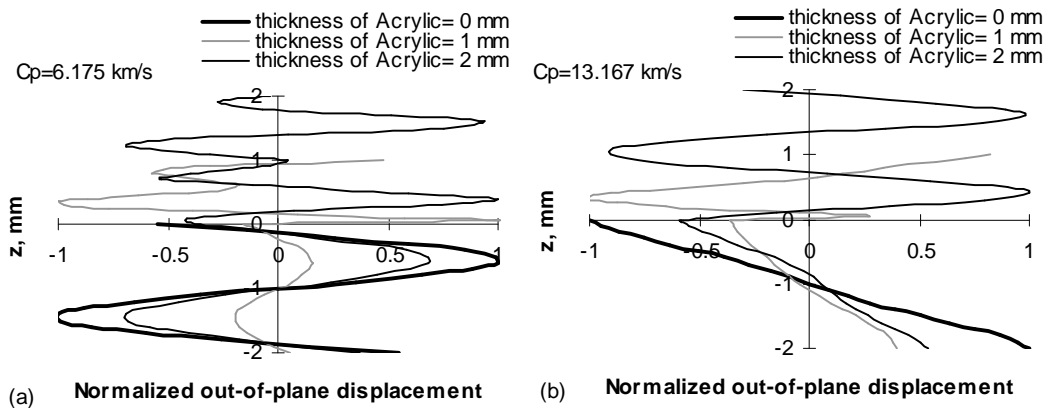


Figure 4: Out-of-plane displacement for an Aluminum plate laminated by Acrylic layers with thickness of 0, 1 and 2 mm

Experimental Procedures

For the experimental trials a Aluminium plate, having 2 mm thickness, with specifications as shown in Figure 5, were provided. Plate was performed with notch defects, with 0.5 mm width and 10%, 30% and 60% of through wall depth as reference defects. Immersion test was used for measuring the real phase and group velocity of different modes of lamb wave propagated in plate. By changing the incident angle in water some peaks were appeared which some of them related to longitudinal wave propagation in water and others referred to ultrasonic lamb wave modes (s_1 mode appeared in 14° and a_1 mode appeared in 17° and a_0 and s_0 overlapped in 30°). In most studies s_0 and a_0 modes have been applied for studies, but in the present work, a_1 and s_1 modes have been used for evaluation.

Two techniques have been applied for inspections: 1) pulse-echo by considering the a_1 mode and using a variable angle probe, as shown in Figures 6a and 2) emission method with s_1 mode as transmitter and receiver and using two normal probe, as shown in Figure 6b. Emission method is similar that pitch-catch technique but two normal probes are applied instead of angle probes. Emitted normal wave causes guided wave propagation when thickness of plate is enough small, due to resonance effect and polarisation of bulk wave in the top and bottom surfaces of plate.

In the present investigation, some experiments were made for studying the ability of these methods for interpretation of notch defects, having different depths. A 5 cycle of sine wave was excited at the 2 MHz was used for examinations. The nominal center frequency of normal and angle transducers was 2 MHz. A fast Fourier transform was used for determining the real frequency of received signal, as shown as a sample in Figure 6.

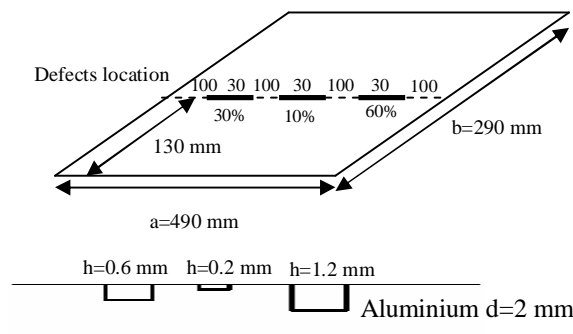


Figure 5: The schematic mapping of fabricated Aluminum plate

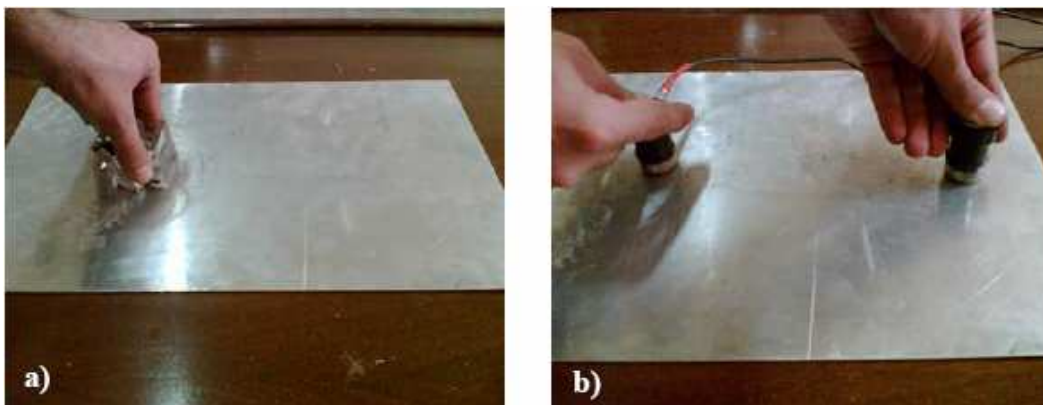


Figure 6: The lamb wave testing methods: a) pulse-echo technique and b) emission method

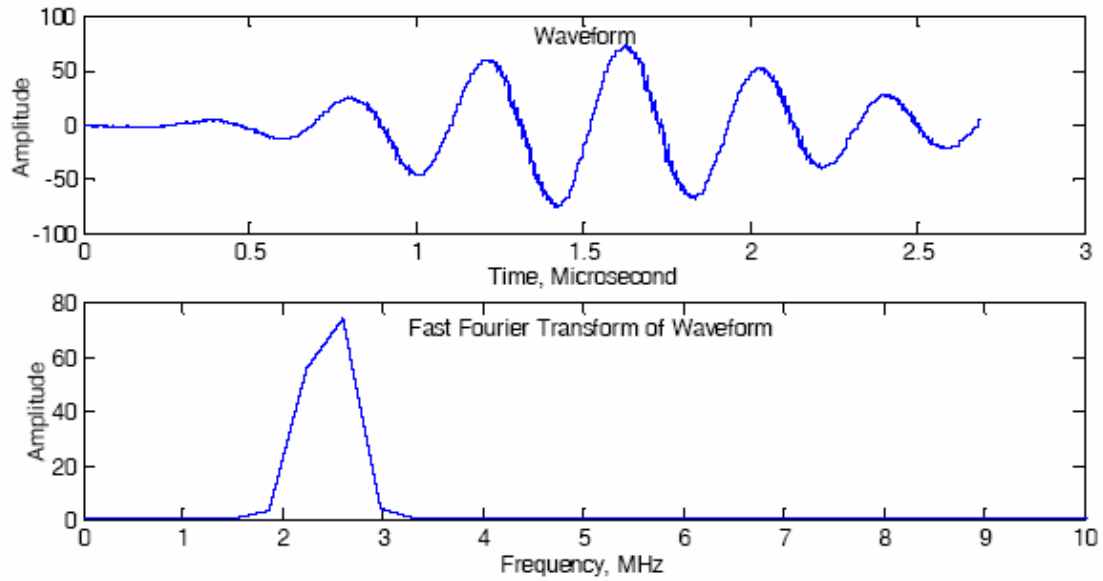


Figure 6: A received waveform and its fast Fourier transform, showing the peak of frequency at 2.6 MHz

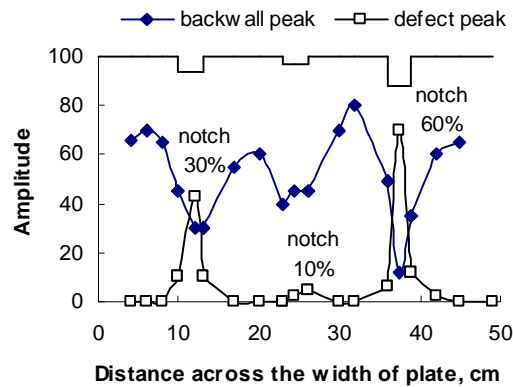


Figure 7: The change of Amplitude of a_1 mode, as scanned plate width (defect to probe distance was 75 mm)

Results and Discussions

The amplitude values which obtained by scanning the width of plate in a pulse-echo method have been shown in Figure 7. There is a powerful backwall peak in the flawless areas. When probe reaches near the defect, amplitude of backwall peak decreases, due to beam spread. In defected zone, backwall peak become weak and a second peak appears. Second peak relate to reflection from defects. When defect depth increases, the reflecting surface increases, so, as seen in Figure 8, back wall peak will be weaker and defect peak will be stronger.

Time of flight and group velocity can be used for determining the location of defect. Group velocity may be calculated by dispersion curves or by assessment the backwall peak and self calibration (if the back wall reflection exists) as is followed:

$$L_d = V_G \cdot t_{of} = \frac{L_b}{m_b} m_d \quad (2)$$

where V_G is group velocity of lamb mode, t_{of} is time of flight of signal related to defect, L_d and L_b are respectively the location of defect and backwall and m_d and m_b are the location of defect and backwall peaks on the time base axis of ultrasonic flaw detector screen. The results of measuring the defect and backwall location, measured by assessment the theoretical group velocity, are shown in Figure 9. It is observed that distance calculations are in a good agreement with real values.

The waveforms of emission method have been shown in Figure 10, indicating that receiver peak will become weaker when a defected zone is scanned. Also, it reveals that increased depth of defects resulting in a more decreased of amplitude. In the emission method defect location can not be determined directly by analysis the waveform. But location of defect may be determined practically by connecting an Acrylic specimen in the beam direction as damper block. Amplitude decreases by connecting the damper block but in a defected zone higher decreased is occurred in comparison with the flawless areas. The location of defects can be found with an acceptable precision by this method.

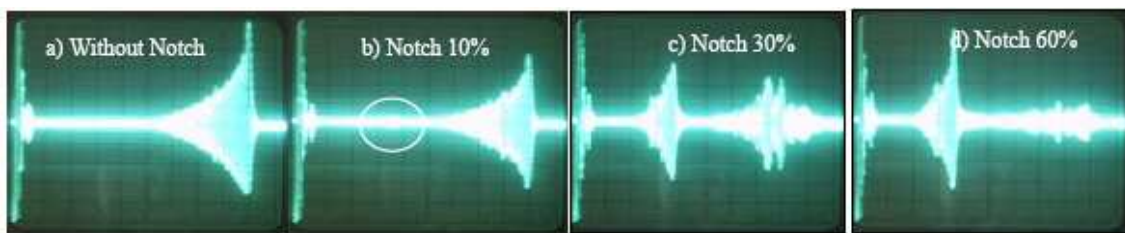


Figure 8: The waveforms of ultrasonic lamb wave in pulse-echo technique, a_1 mode evaluated (defect to probe distance was 75 mm)

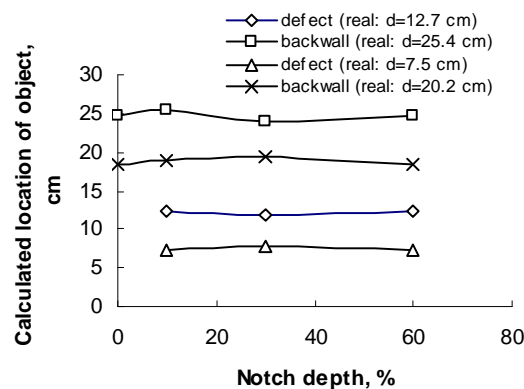


Figure 9: The result of calculated location of object as compared with real values

Defect sizing is more difficult in ultrasonic lamb wave testing, due to its dispersive nature. In thin plates happily, it is usually important to flaw detecting and defect sizing isn't necessary in many cases. In lamb wave testing, defect length may be measured similar that one in bulk wave ultrasonic flaw detecting (6 db drop low). This means that the start and end points of a defect can be calculated where the peak intensity of defect shows a 6 db decrease. But height and depth of defects, detected by lamb wave, can not be measured by the common defect sizing methods. Amplitude in ultrasonic lamb wave testing gives some qualitative information about defect depth. The variations of amplitude as a function of defect depth, when using different ultrasonic lamb wave testing techniques, have been shown in Figure 11. It seems that in pulse echo method, the change of amplitude is more sensitive to defect depth than two other techniques.

We used a notch defects as references for testing. A Distance-Amplitude-Correction curve (DAC) was made for evaluation. This diagram, as shown in Figure 12, has three curves relating to notches of 10%, 30% and 60%. The

observed signal in Figure 12 related to a notch with 50% depth. It was observed that defects could be evaluated with good precision by drawing the DAC. This method is easy for applying by operators and can be used in the similar way of common ultrasonic testing methods. Experiments showed that notch defects with the depth of 10% and higher could be evaluated by used methods. Unfortunately, the amplitude analysis wasn't sometime repeatable. Inspection was more difficult when probe to defect distance increased, due to attenuation, dispersion, beam speared effects and increased pulse duration. For long range inspections, low frequency probes should be used. These methods were fast and a large area of plates was inspected in a short time.

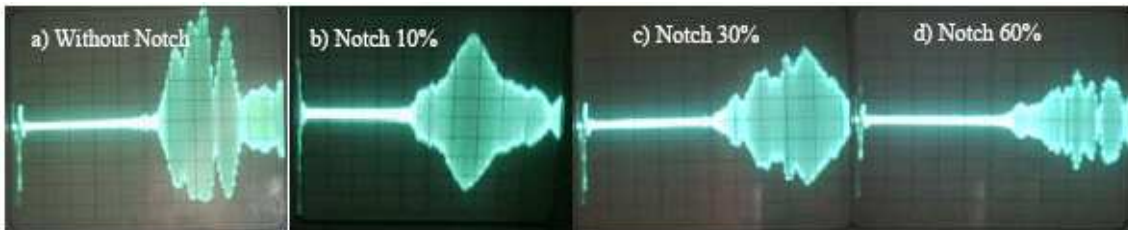


Figure 10: The waveforms of ultrasonic lamb wave in emission technique, s_1 mode evaluated (defect to transmitter distance and defect to receiver distance was 50 mm)

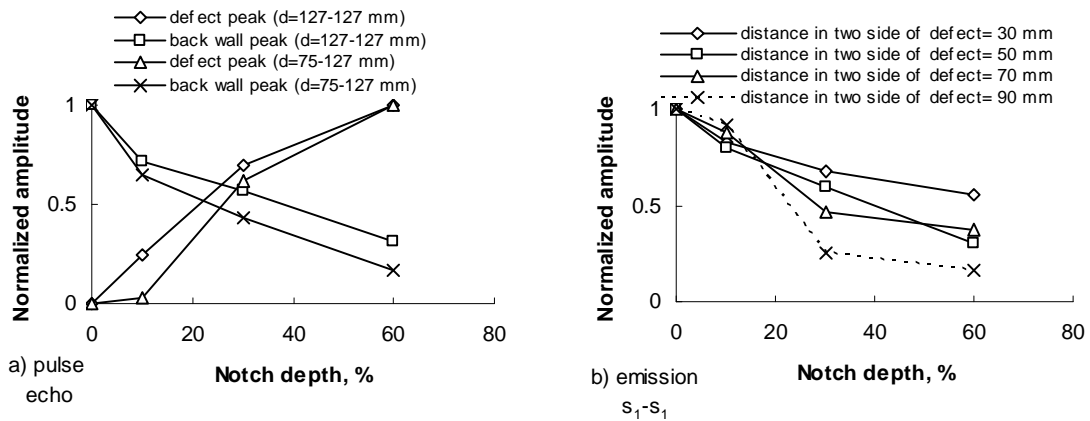


Figure 11: The variations of normalized amplitude values as a function of defect depth in: a) pulse-echo method and b) emission technique

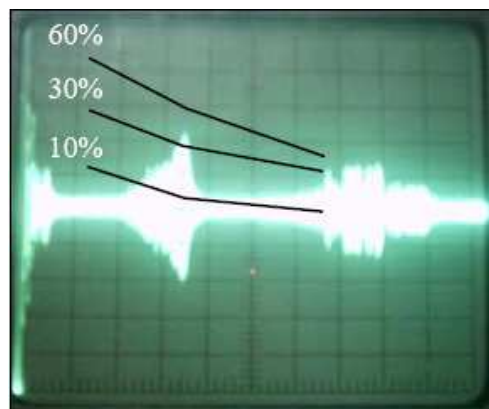


Figure 12: The Drawing the DAC curve for defect evaluating by assessment the notch defects with the depth of 10%, 30% and 60% as reference defects

Conclusions

In the present work pulse-echo and emission lamb wave testing methods were used for interpretation of notch defects (10-60% of through wall depth) and s_1 and a_1 modes were considered for inspections. It was found that these techniques could detect all fabricated defects. Inspection was more difficult as the probe to defect distance increased. Amplitude analysis showed that defect depth could be evaluated by drawing the DAC curves. Pulse echo was more sensitive for defect detection than emission technique. Location of defects was found by assessment the group velocity in pulse echo technique and the length of defect was determined by the law of 6 db drop.

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Appendix

The followed equation can be used for predict the lamb wave phase velocity (C_p) in a plate:

For symmetric modes:

$$\frac{\tan(qd/2)}{\tan(pd/2)} = \frac{-4k^2 \cdot pq}{(q^2 - k^2)^2}$$

For antisymmetric modes:

$$\frac{\tan(qd/2)}{\tan(pd/2)} = \frac{(q^2 - k^2)^2}{-4k^2 \cdot pq}$$

Where k is wave number of lamb wave and is given by:

$$k = \frac{2\pi f}{C_p}$$

p and q are calculated by:

$$p = k^2 - \left(\frac{2\pi f}{C_L}\right)^2 \quad \& \quad q = k^2 - \left(\frac{2\pi f}{C_T}\right)^2$$

f = linear frequency of lamb wave; ω = angular frequency = $2\pi f$; C_L = longitudinal ultrasonic bulk wave velocity;

C_T = shear ultrasonic bulk wave velocity; d = thickness of plate

Group velocity (C_G) predicts as followed:

$$C_G = C_p \cdot \left(1 - \frac{1}{1 - \frac{C_p}{\alpha}}\right) : \alpha = fd \frac{dC_p}{d(fd)}$$